



M2lines

# Deterministic and Stochastic Tendency Adjustments Derived from Data Assimilation and Nudging

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*U.S. NSF National Center for Atmospheric Research*

Mar, 2024

# Co-Authors

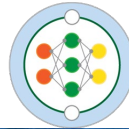


Judith Berner

**Special thanks:** Kevin Raeder, Jeff Anderson , Patrick Callaghan

# Funders

M2lines



SCHMIDT **FUTURES**

## M<sup>2</sup>LInES - Multiscale Machine Learning In Coupled Earth System Modeling

M<sup>2</sup>LInES (pronounced M-square-lines) is an international collaborative project with the goal of improving climate projections, using scientific and interpretable Machine Learning to capture unaccounted physical processes at the air-sea-ice interface.

## Recent Publication:

Quarterly Journal of the  
Royal Meteorological Society



RESEARCH ARTICLE

# Deterministic and Stochastic Tendency Adjustments Derived from Data Assimilation and Nudging

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PDF



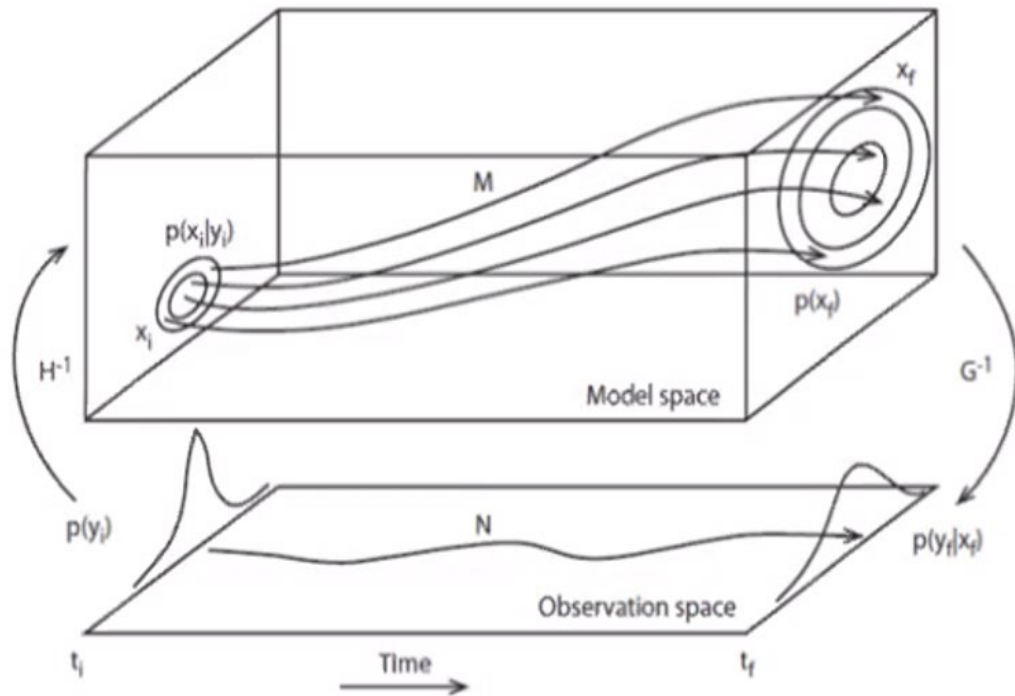
TOOLS



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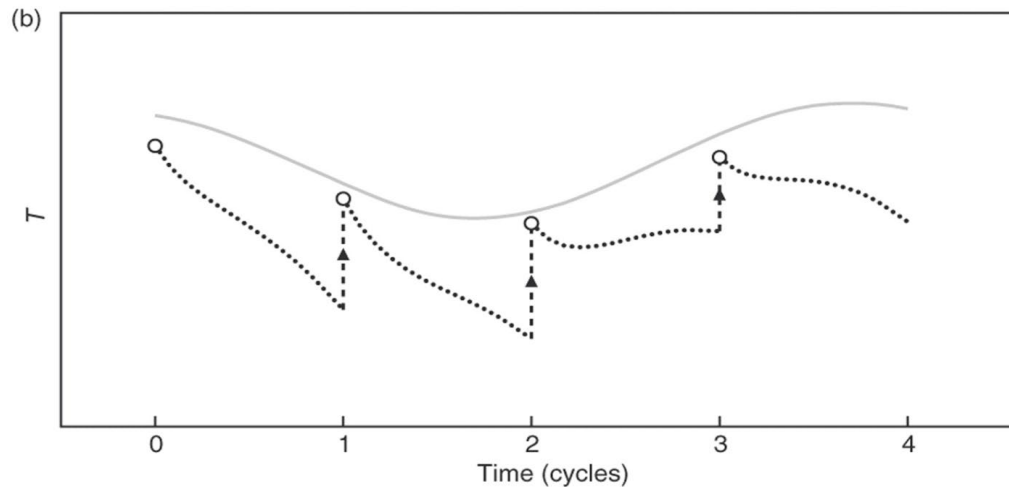
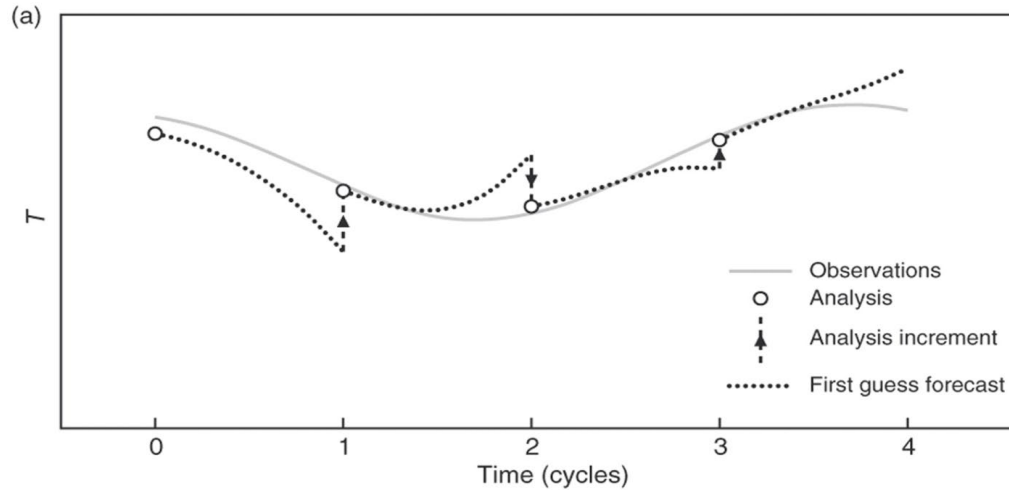
# Background - Data Assimilation



- DA combines a model first guess (a short model forecast) with observations in an optimal way for the purpose of state-estimation and initialization
- Observations will “pull” the model trajectory closer to the observed trajectory

Balmaseda, Magdalena A. "Data assimilation for initialization of seasonal forecasts." *Journal of Marine Research* 75.3 (2017): 331-359.

# DA used to Identify Systematic Model Error

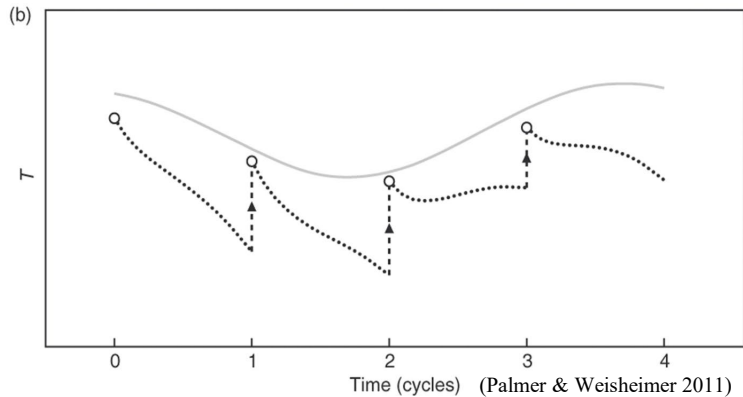


- **Schematic:** *The analysis increment is correcting the model trajectory systematically (averaged over many initializations) to a warmer state.*
- *This is evidence of a systematic model error (assuming unbiased obs)*

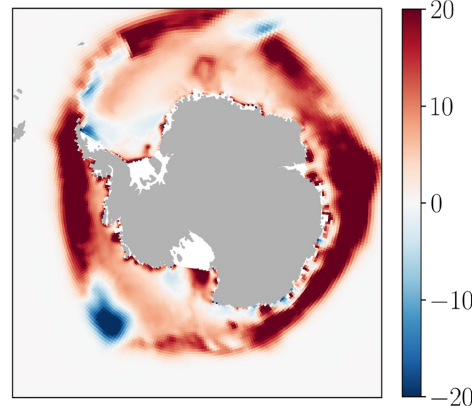
Palmer, T. N., and Antje Weisheimer.  
"Diagnosing the causes of bias in climate models—why is it so hard?." *Geophysical & Astrophysical Fluid Dynamics* 105.2-3 (2011): 351-365.

Although the amplification of the effect of [INSERT FORCING] on [INSERT BIASED PROCESS] will occur on ***timescales of decades***, the intrinsic timescale associated with [INSERT BIASED PROCESS] itself is typically on the order of hours. Hence it should in principle be possible to assess whether the anomalously small values of [INSERT PROCESS] are realistic or not, by studying the performance of such models in short-range weather prediction mode.

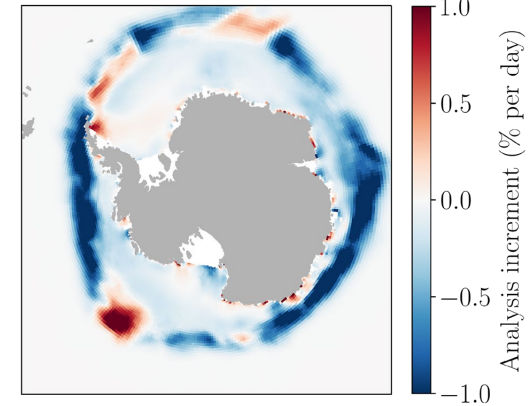
## biased model



## BIAS



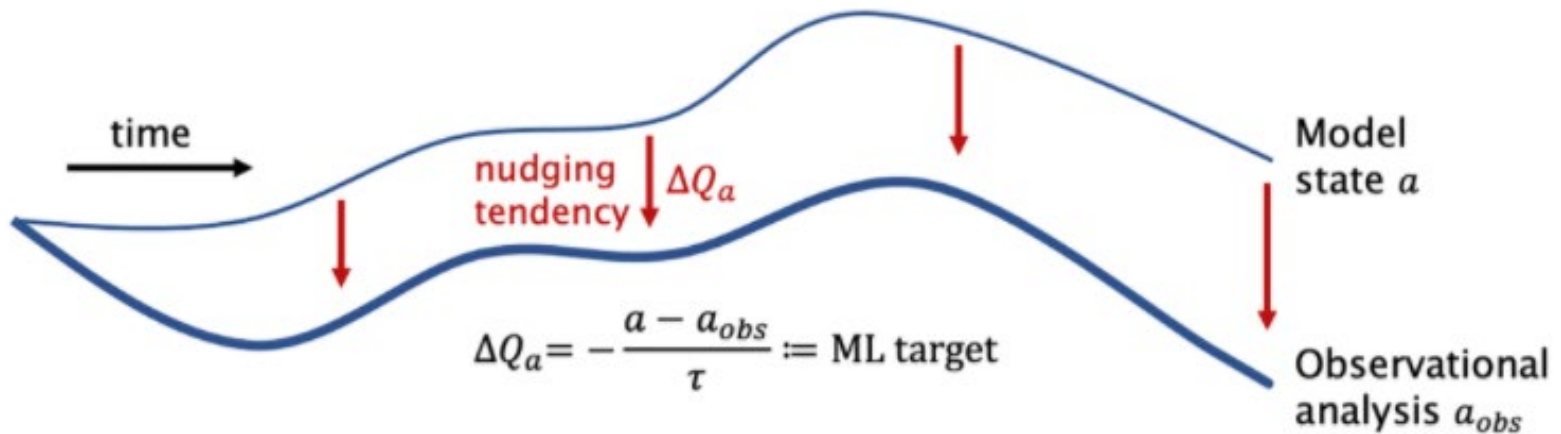
## Avg. Increment



Gregory, William, et al. "Deep learning of systematic sea ice model errors from data assimilation increments." *Journal of Advances in Modeling Earth Systems* 15.10 (2023): e2023MS003757.



# Nudging

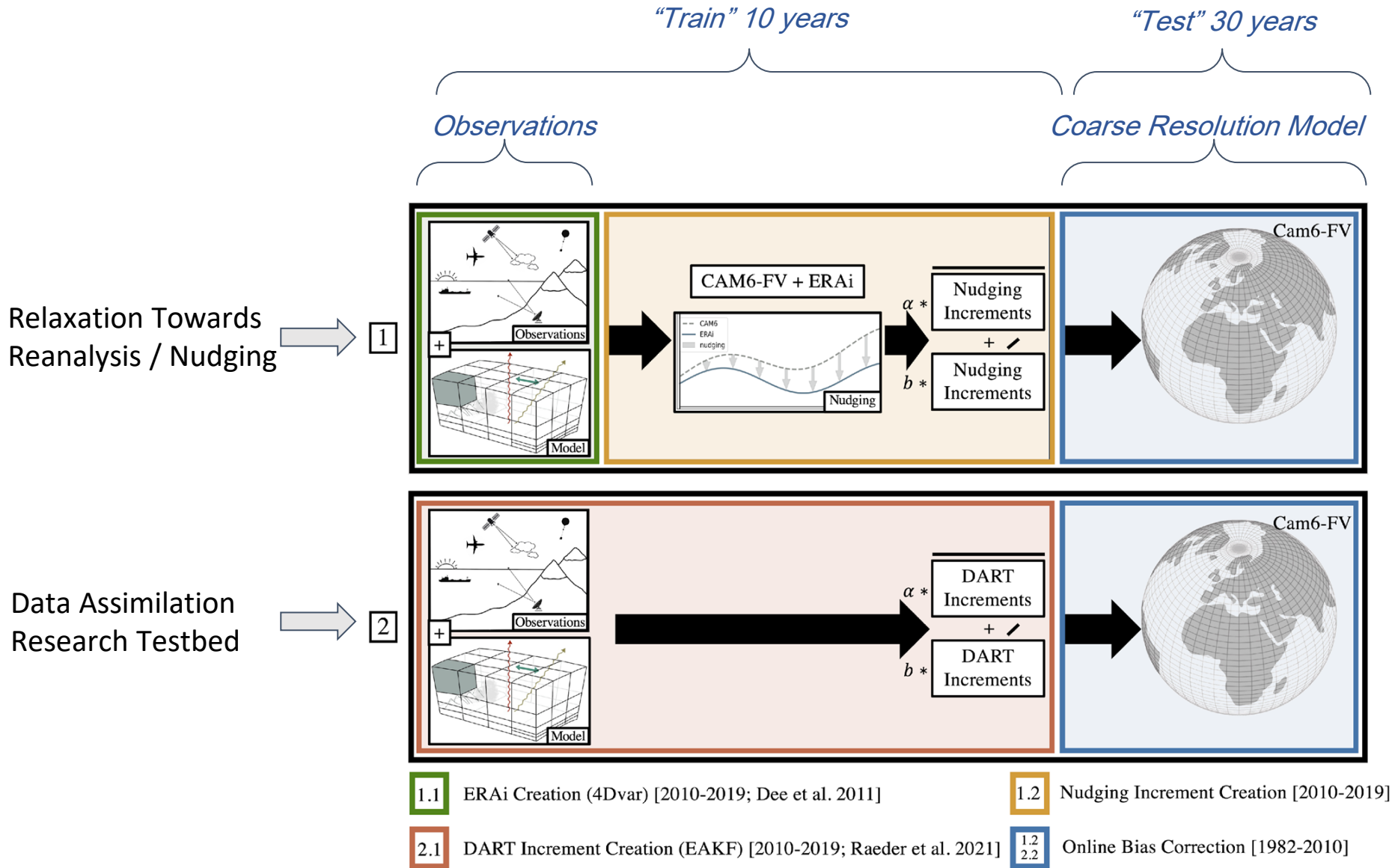


Watt-Meyer, Oliver, et al. "Correcting weather and climate models by machine learning nudged historical simulations." *Geophysical Research Letters* 48.15 (2021): e2021GL092555.

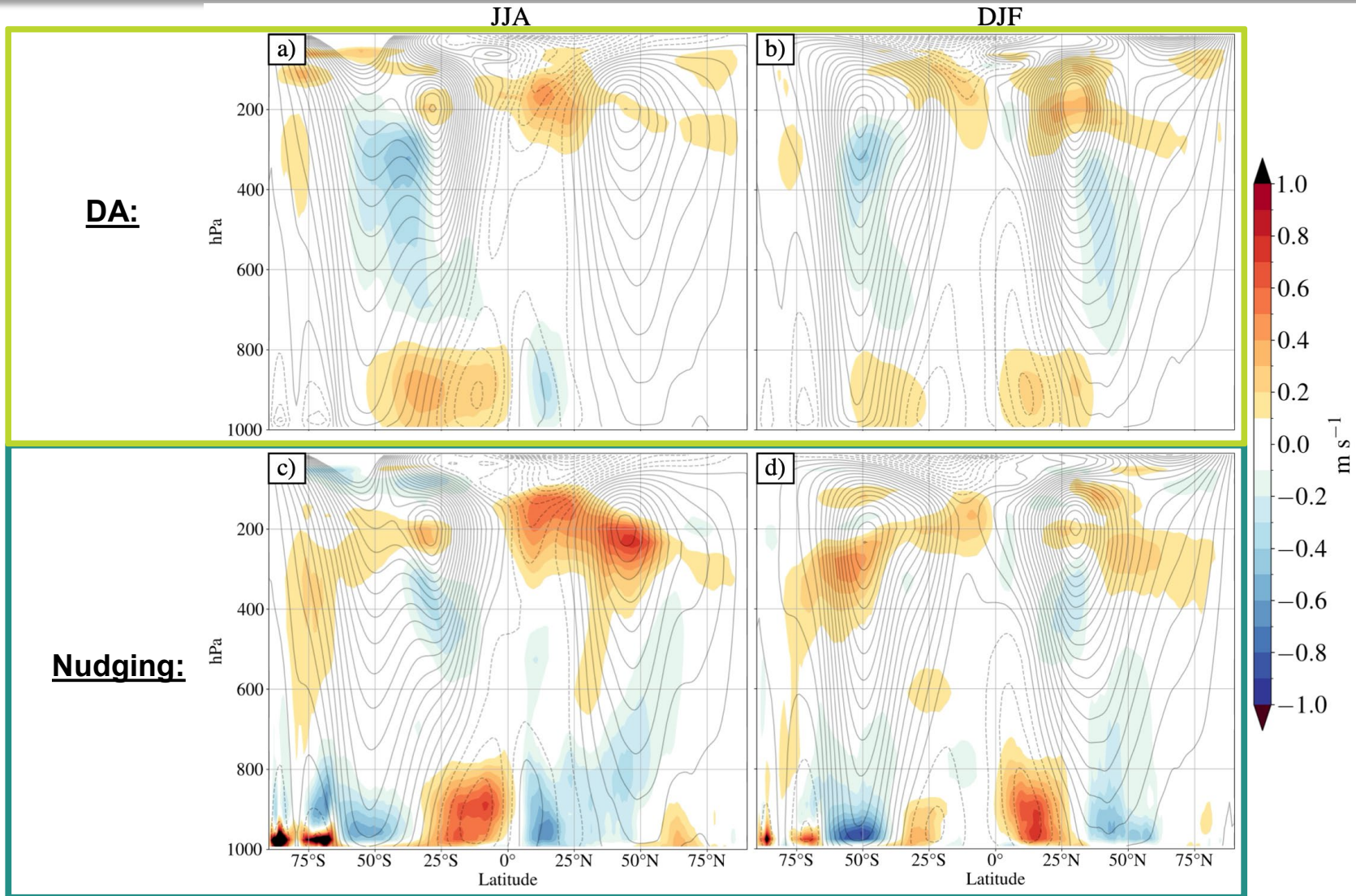
A linear relaxation term is added to the prognostic equations of certain variables. Where  $a$  is a prognostic variable,  $-v \cdot \nabla a$  is advection by the model.



# Two Error Learning “Pathways”





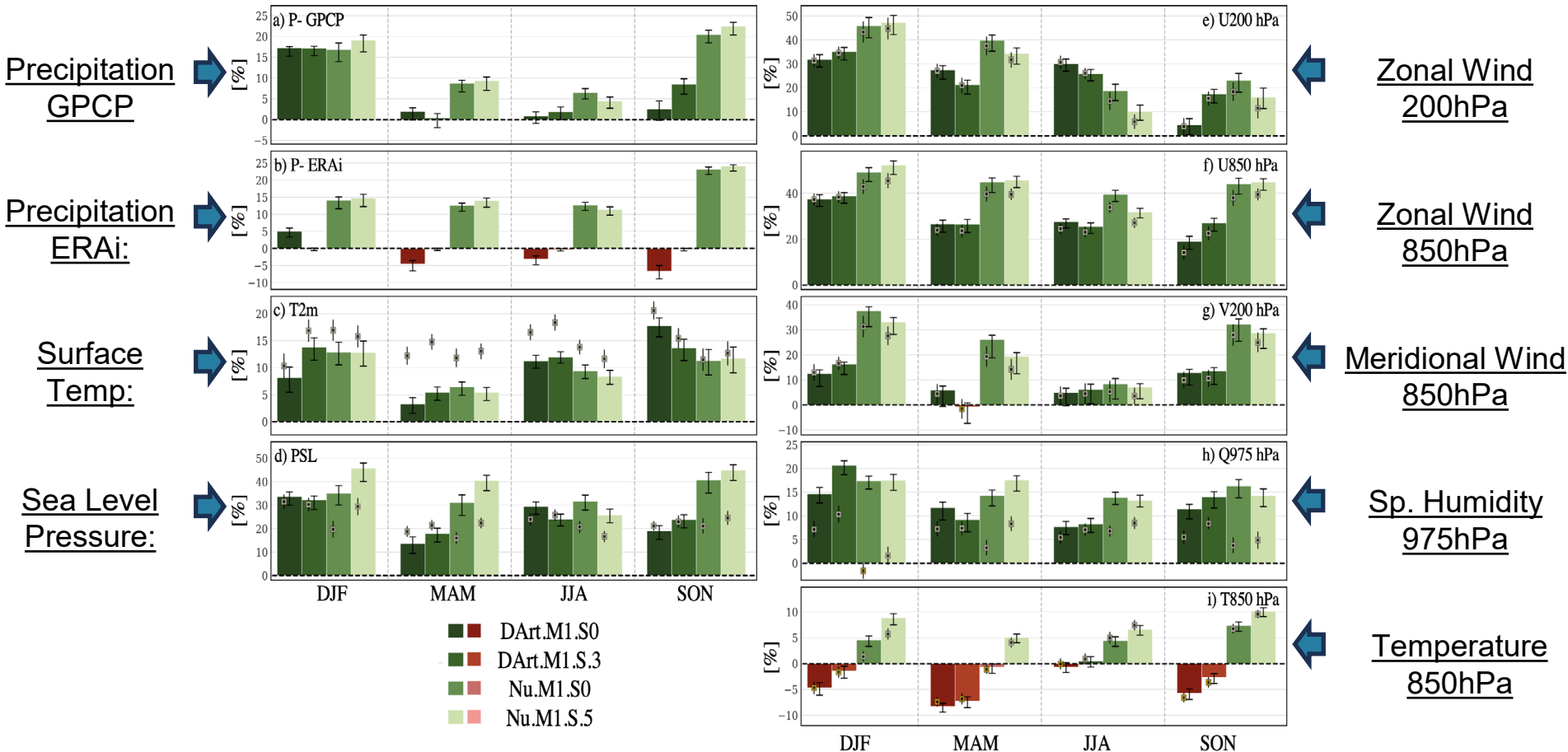


**FIGURE 3** The zonal-mean  $u$  DA increments ( $m s^{-1} d^{-1}$ ) in JJA (a, c) and DJF (b, d) for the DART (Row I) and nudging system (Row II). Contours show the  $u$  wind climatology [ $2 m s^{-1}$  intervals, negative is dashed]. All fields are averaged over the period 1982-2010.



To what extent does re-inserting DA increments and nudging increments during model runtime **reduce climatological model bias** of the free-running model?

CAM has **STRONG** biases in Precipitation and this is common across many models



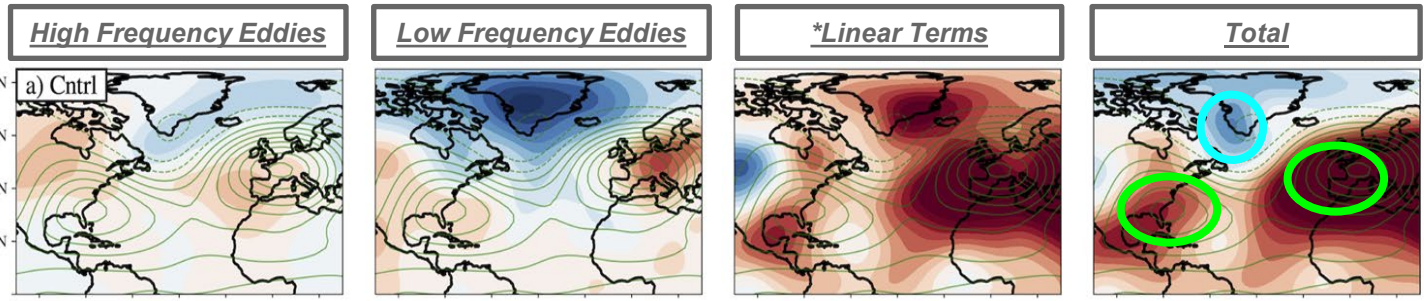


Will representing subgrid-scale uncertainty in online increment corrections via *stochasticity* help to improve low-frequency modes of variability without degrading mean state climatological bias?

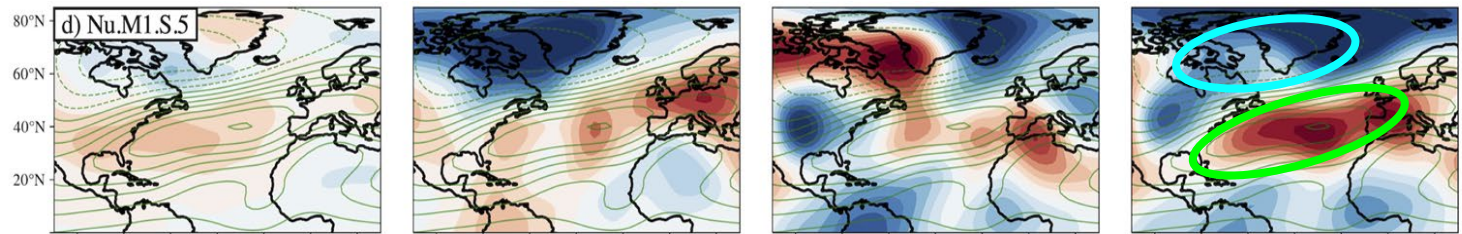
### NAO Stream Function Tendency Decomposition (10-1 day before peak event):

Forcing from:

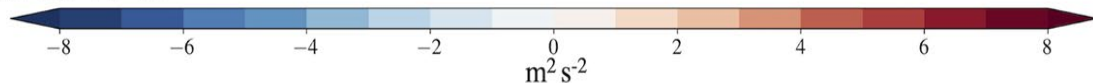
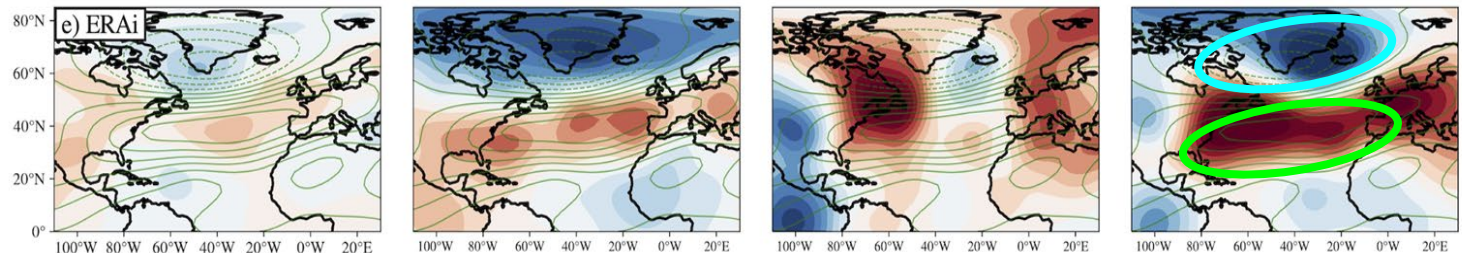
Control



Stochastic +  
Deterministic  
Tendency  
Adjustment



ERA Interim

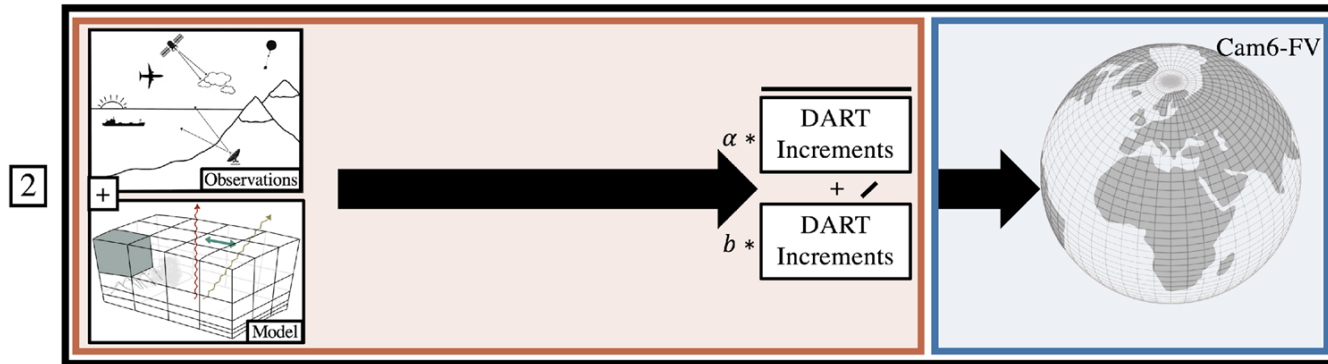


\*Linear Terms: Planetary vorticity advection by the anomaly + interaction of anomaly with zonal mean climo. flow + divergence term.



- We find that the nudging increment adjustment outperforms the correction provided by the DART increments (*but only just*).
- A disadvantage of the DA increments is that they **depend on observations which are spatially inhomogeneous and can be sparse**. Especially in data-limited regions, the analysis increment will unlikely represent model-error.
- On the other hand, nudging increments will benefit from the balance and conservation properties inherent in reanalysis as well as the spatial homogeneity of a gridded product. A noted **disadvantage of the nudging tendencies is that the model will adopt the same biases present in the reanalysis**.
- While the exact computational cost is system-specific, all data assimilation systems are resource-intensive. Indeed, they are often not readily available, **which makes an online -bias correction based on nudging tendencies a viable and flexible approach to study the impact of model bias in climate models**.





1.1 ERAi Creation (4Dvar) [2010-2019; Dee et al. 2011]

1.2 Nudging Increment Creation [2010-2019]

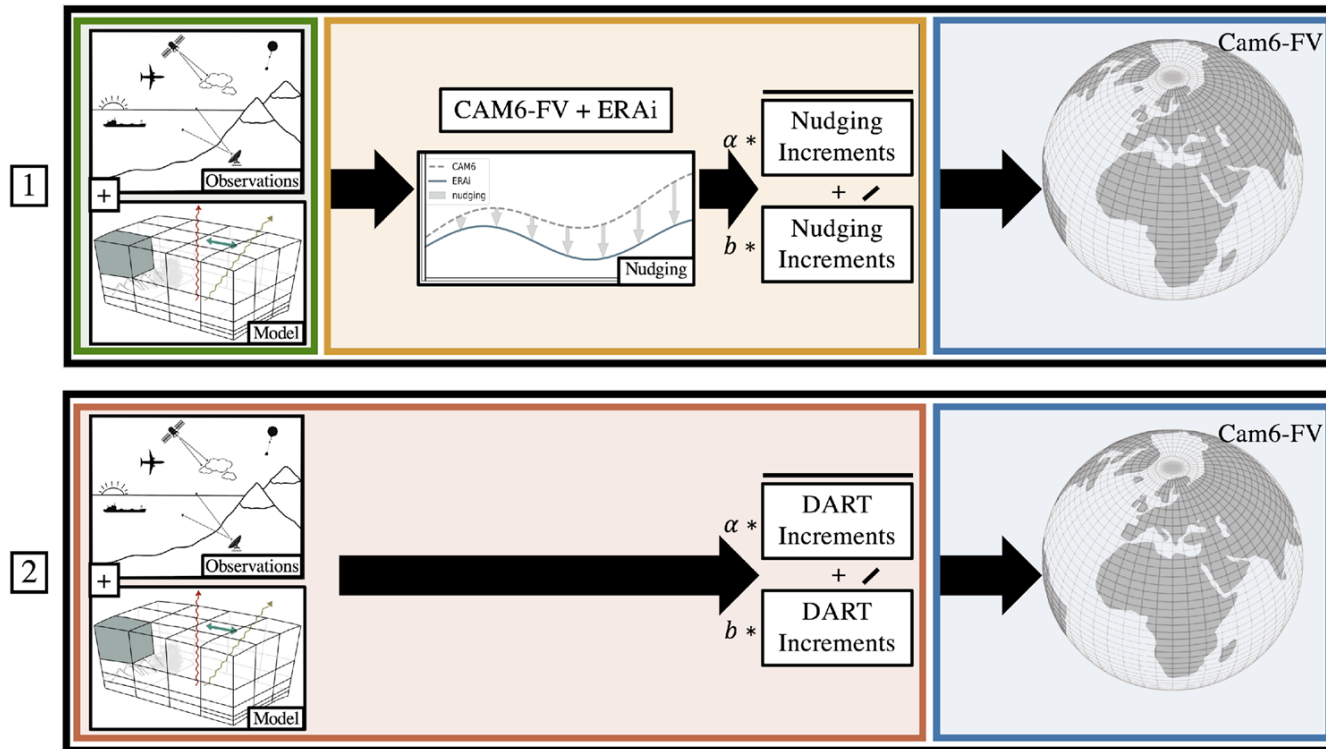
2.1 DART Increment Creation (EAKF) [2010-2019; Raeder et al. 2021]

1.2  
2.2 Online Bias Correction [1982-2010]

- Nudging increments and DA increments pick up the same general features of systematic model bias, particularly in the tropics at lower model levels
- Overall, we find a positive impact of an online model -error representation based on re-inserting DA increments and nudging on the climatological bias.
- The addition of a stochastic tendency reduced this bias and created an more accurate representation of major modes of variability when compared to observations.



Can this process be replaced with a Machine Learning pipeline to create a “state-dependent” correction?



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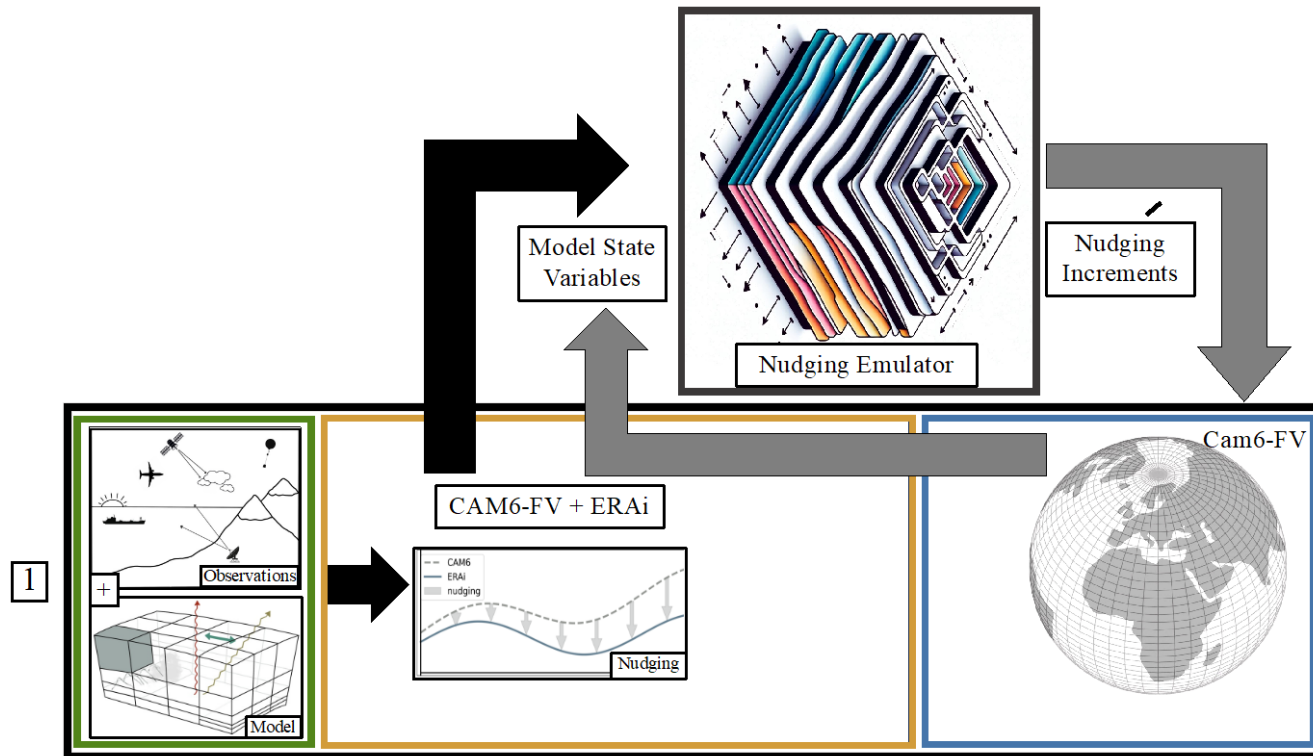
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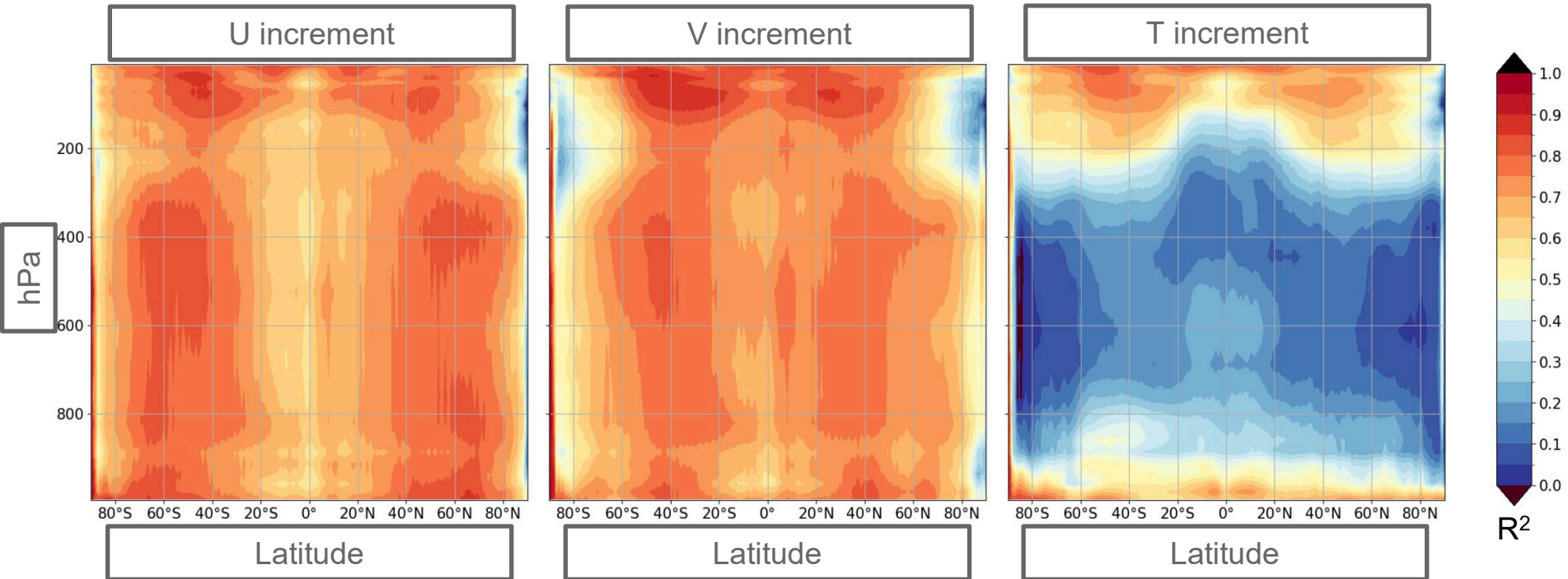


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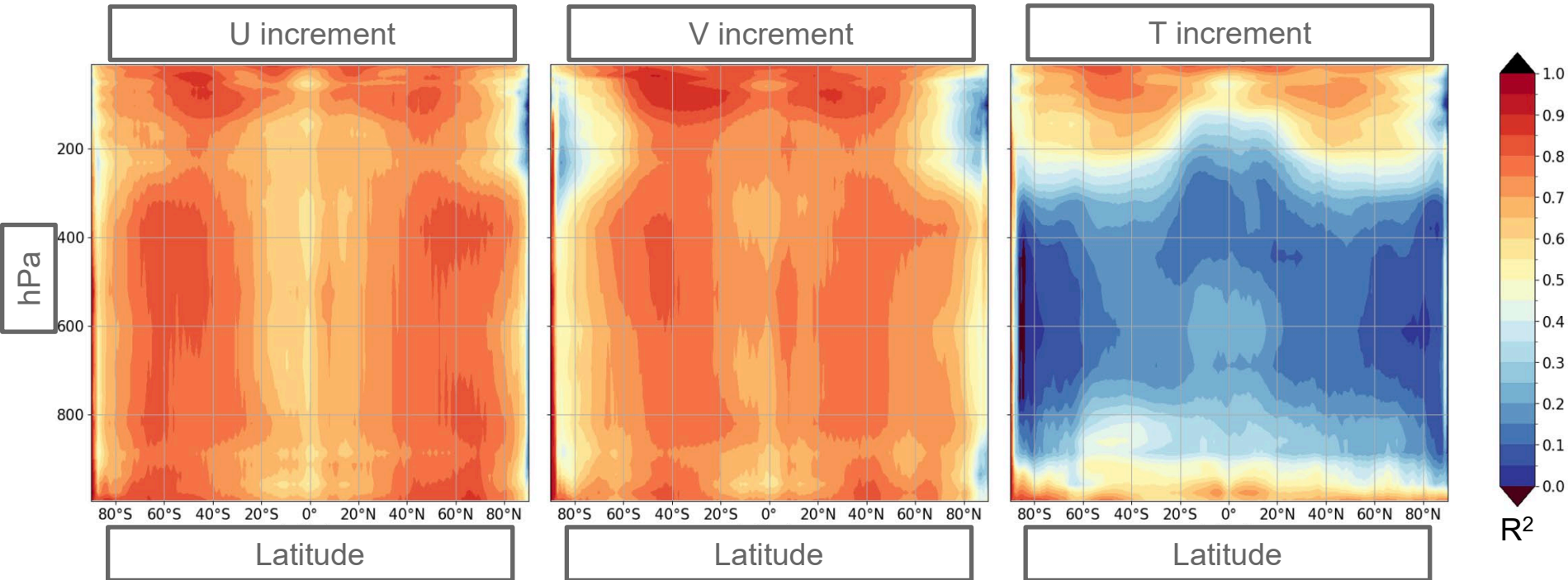
1.2 Nudging Increment Creation [2010-2019]

1.3 Machine Learning Emulator

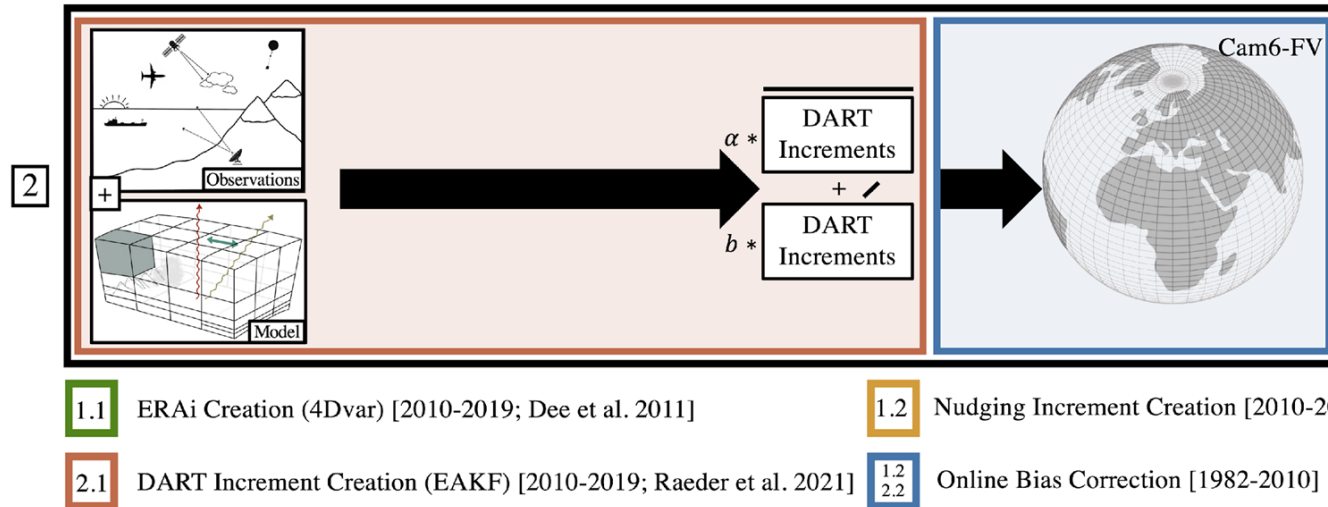
1.4 Online Bias Correction [1982-2010]







**Results are pending in online simulation!**



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