The geometry of parameter space in standard and ultra-low resolution CESM PPEs







Sanderson et al. 2008

June 2024, CESM Workshop - AMWG

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How to constrain climate projections with observational data given the huge dimension of parameter space?



 $\sim \mathcal{O}(1000)$ parameters

Do We need to Know the Value of all Climate Model Parameters?



 $\sim \mathcal{O}(1000)$ parameters

Simple Questions Lead To Simple Models?



Importance to prediction of parameter combination

Transtrum and Qiu 2014

Sloppiness: Importance to Precdictions Decay Exponentially



Quinn et al. 2022

Fisher Metric: How much can we tell models apart?

$$\mathscr{I}_{i,j}(\theta) = \mathbb{E}[\partial P(\theta) / \partial_{\theta_i} \cdot \partial P(\theta) / \partial_{\theta_j}]$$

Fisher Spectrum Importance to prediction of parameter combination Transtrum and Qiu 2014

Sloppyness is Universal



Global and Local Sloppiness

Parameter Hierarchy





Model Widths



Understand Model Variability by Dimensional Reduction



 $\sim \mathcal{O}(1000)$ parameters

Dimensionality Reduction for Climate Predictions

Low Resolution $10^{\circ} \times 15^{\circ}$ Model



Find Low Dimensional Representation



• Explore Behavior manifold & Fisher Metric • Analyze Robustness of predictions

Benchmark low resolution model



EAS

PD and SST4K show alignment of Low Res to High Res Reponse to Parameter Variation



Low Res Captures CMIP6 Variation





Initial sloppiness analysis



Summary

Climate is Sloppy





Looking ahead:



- Find low dimensional representation by identifying stiff directions in parameter space (those that best explain variation)
- Explore climate response using low dimensional representation



- Slab ocean
- Interpret physics of stiff directions
- Analyze robustness of predictions

Thank you



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